



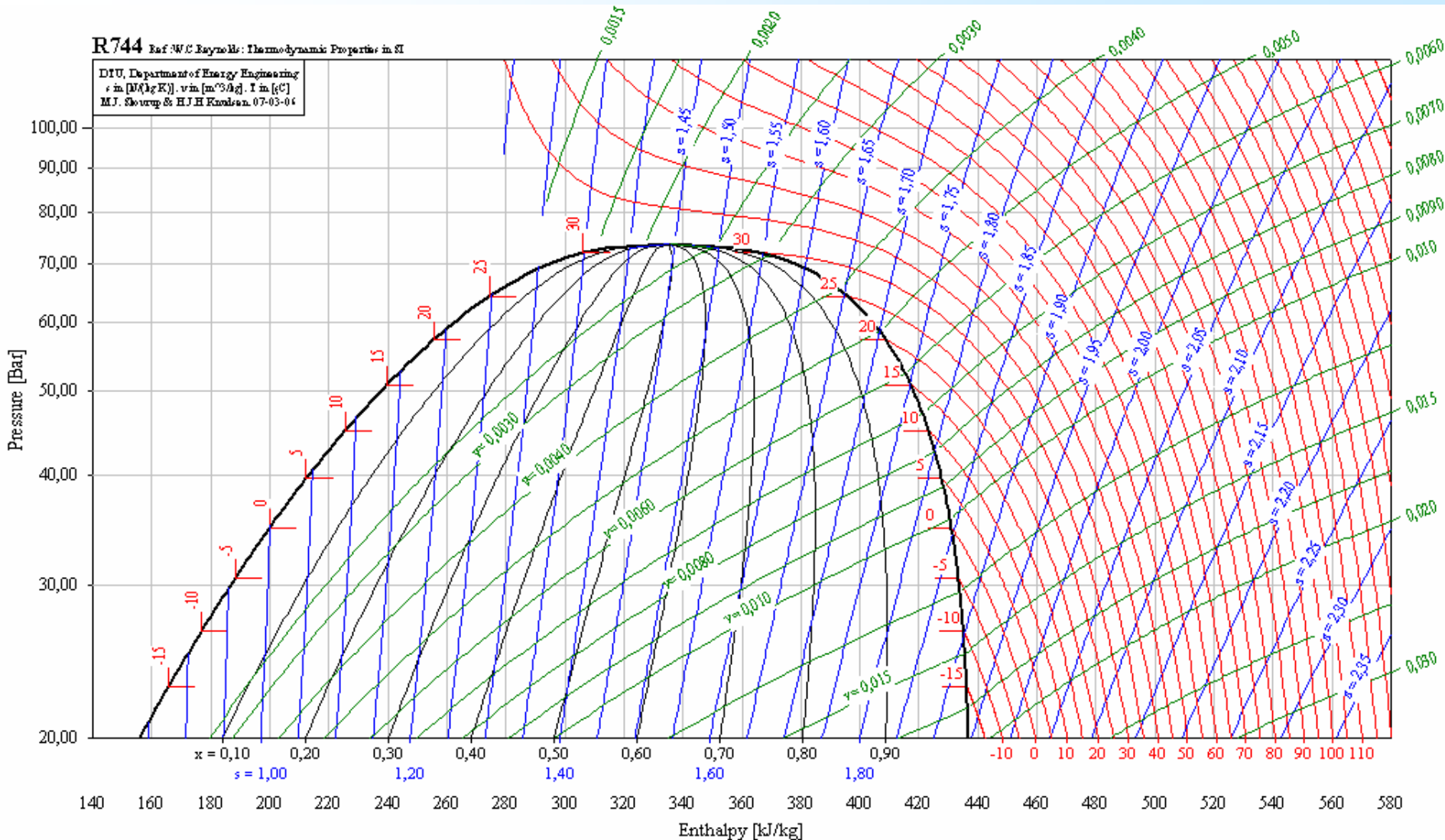
**Study on CO₂
Rankine Cycles
for Low and
Medium
Temperature
Geothermal
Sources for
Power Production
and Cogeneration**

Study on Rankine and Heat cycles for geothermal plants using carbon dioxide as working fluid

The study refers at three types of plants, producing:

- 1. Only electric power*
- 2. Electric power and hot tap water*
- 3. Electric power and district heating*

The CO₂ pressure-enthalpy diagram used for the study of binary and heat cycles



The initial data :

a. Temperature of geothermal source **120°C**

b. Temperature of cooling source:

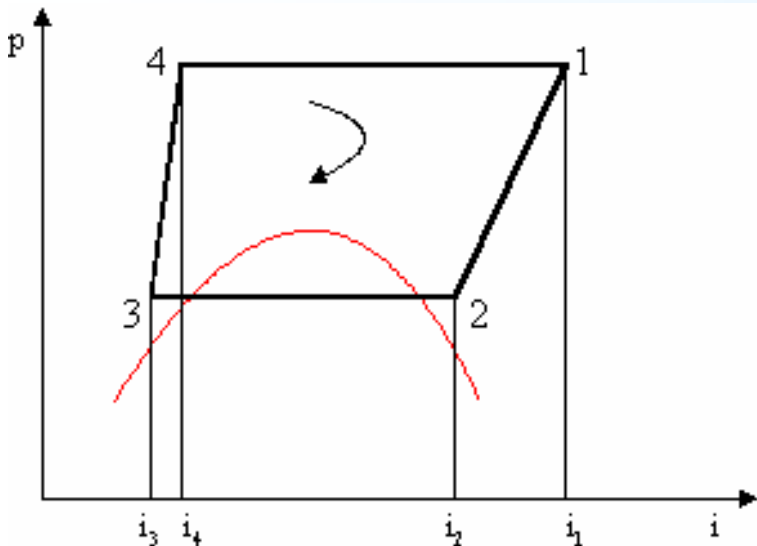
10°C – producing only electric power,

40°C – producing electric power and hot tap water,

50-70°C – producing electric power and heating agent for district heating

c. Working agent **CO₂**

Clausius-Rankine direct cycle



The thermal efficiency of CO₂ power cycle was determined using the well-known formula:

$$\eta_t = \frac{l_{12} + l_{34}}{q_{41}} = \frac{(i_1 - i_2) + (i_3 - i_4)}{i_1 - i_4} = 1 - \frac{i_2 - i_3}{i_1 - i_4}$$

l_{12} – specific work produced in the turbine

l_{34} – specific work consumed in the pump

q_{41} – heat provided by geothermal water

The theoretical global thermal efficiency of CO₂ direct cycle, considering cogeneration of power and heat is 100 %

$$\eta_t = \frac{l_{12} + l_{34} + |q_{23}|}{q_{41}} = \frac{(i_1 - i_2) + (i_3 - i_4) + (i_2 - i_3)}{i_1 - i_4} = \frac{i_1 - i_4}{i_1 - i_4} = 1$$

The *power* efficiency will be determined for all the cycles with the same formula

q₂₃ – heat provided by CO₂ to hot tap water or district heating agents

All cycles are consisting of:

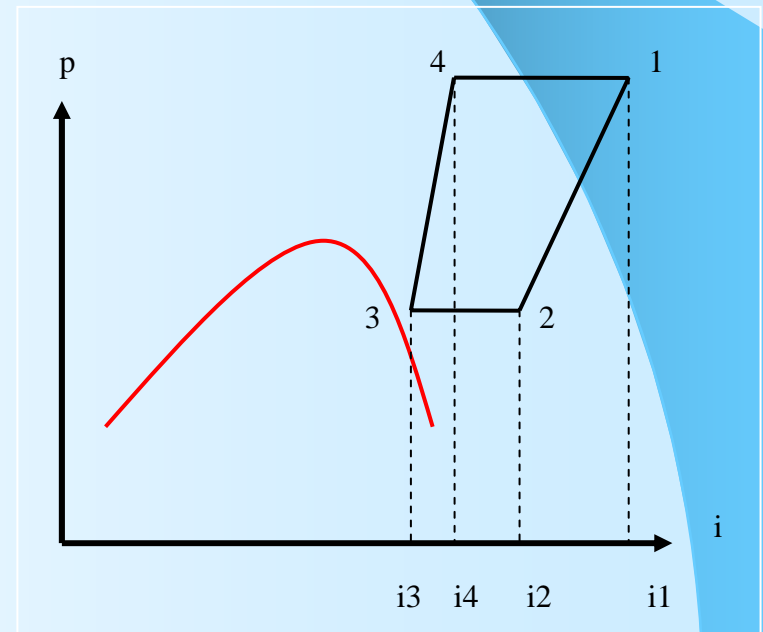
1-2: isentropic expansion

2-3: isobaric cooling

3-4: isentropic compression

4-1: isobaric heating

CO₂ vapour (heat) direct cycle



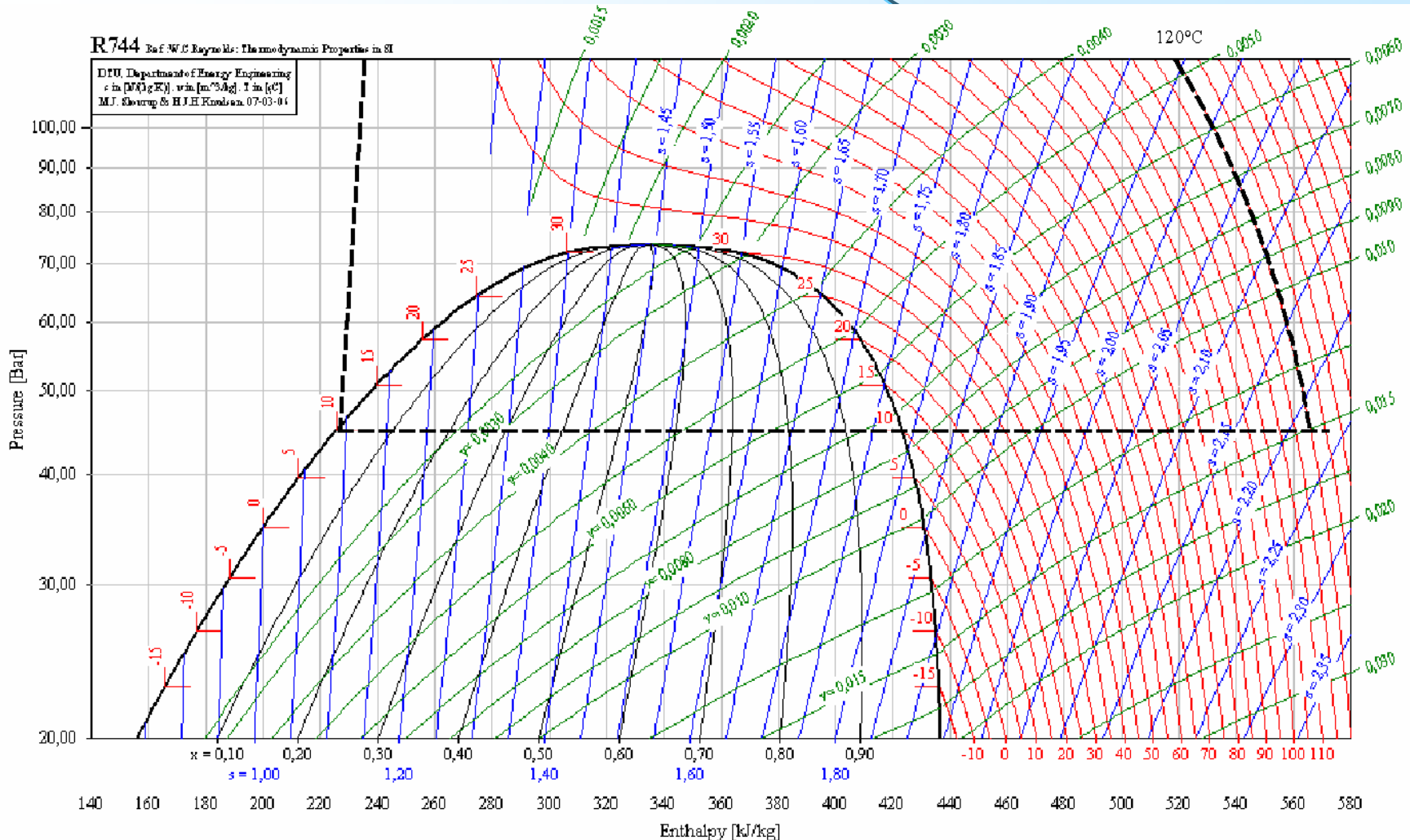
All the studied cycles were limited by following curves:

isothermal curve: $t = 120^{\circ}\text{C}$;

isobaric curve: $p = 120$ bar

isothermal curve: $t = 10^{\circ}\text{C}$;

isobaric curve: $p = 45$ bar



The studied binary cycles, producing only electrical power were limited by following curves:

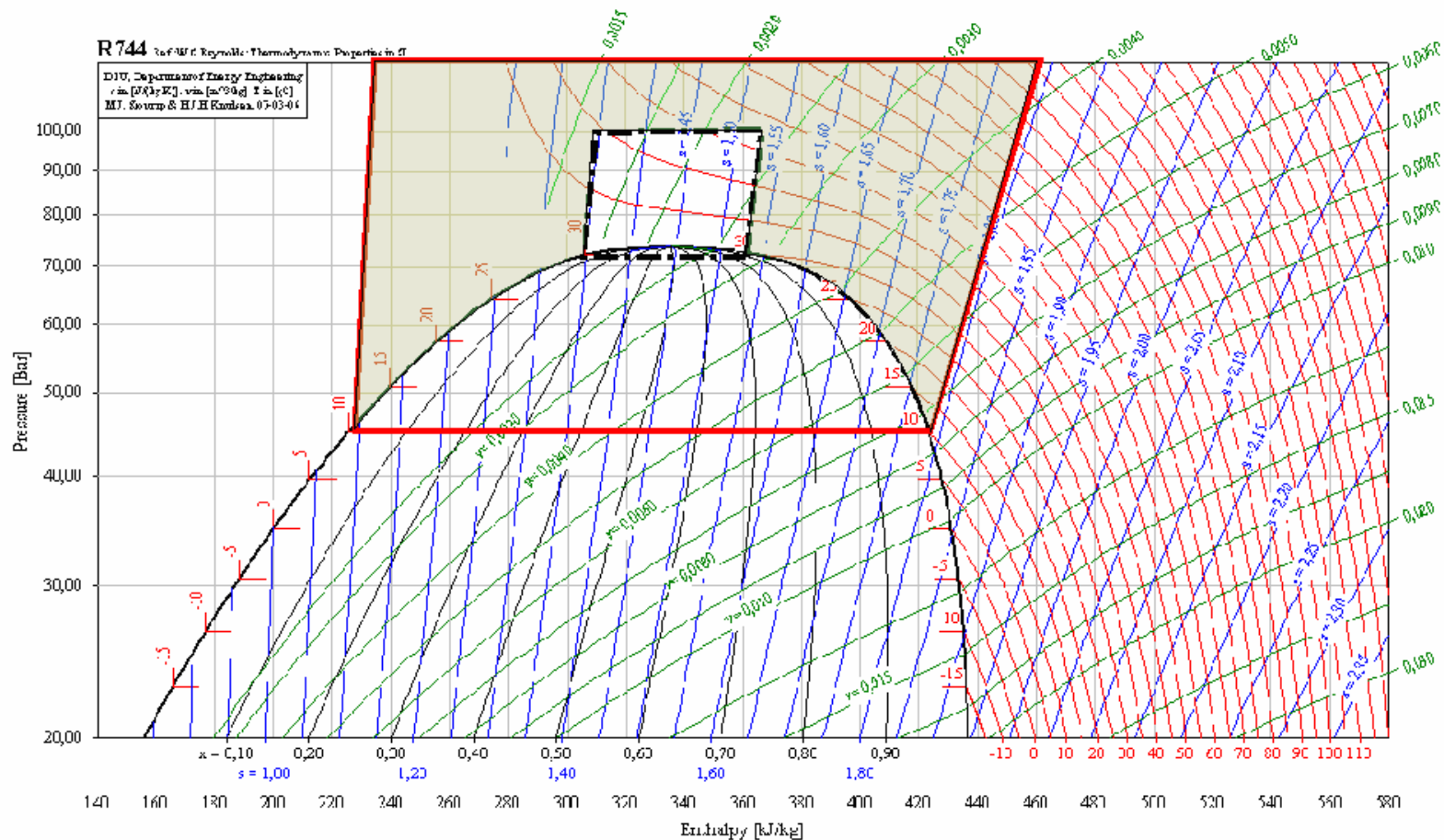
isothermal curve: $t = 115^\circ\text{C}$;

isobaric curve: $p = 120$ bar

isothermal curve: $t = 10^\circ\text{C}$;

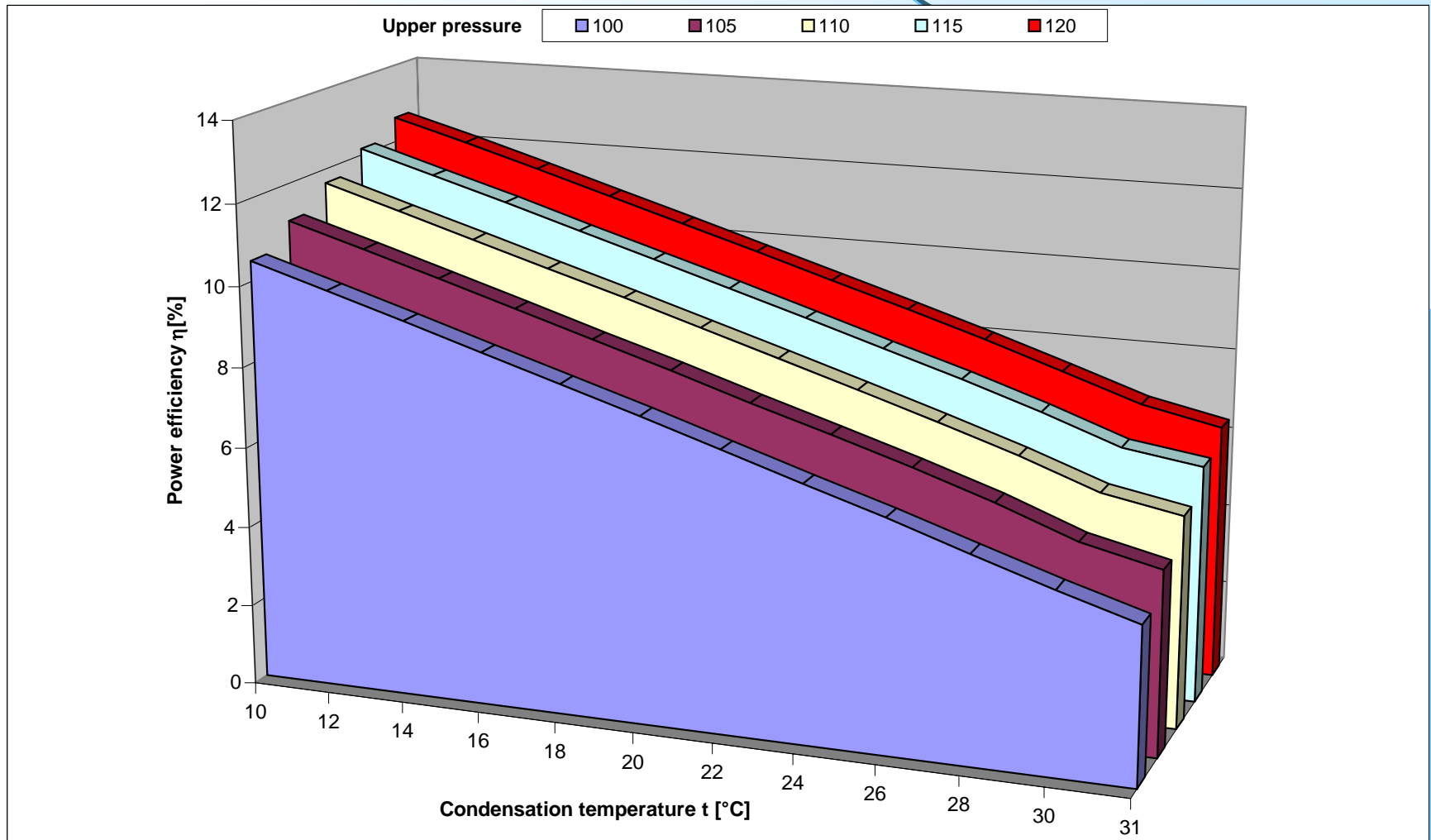
isobaric curve: $p = 45$ bar

The studied parameters was the condensation temperature from 10 to 31 °C, and the upper pressure from 100 to 120 bar



The power efficiency is **increasing** with the growth of upper pressure ($p_1=p_4$) and **lowering** of condensation temperature ($t_3=t_2$)

The maximum efficiency ($\approx 12,5\%$) was provided for upper pressure 120 bar and condensation temperature of $10\text{ }^\circ\text{C}$

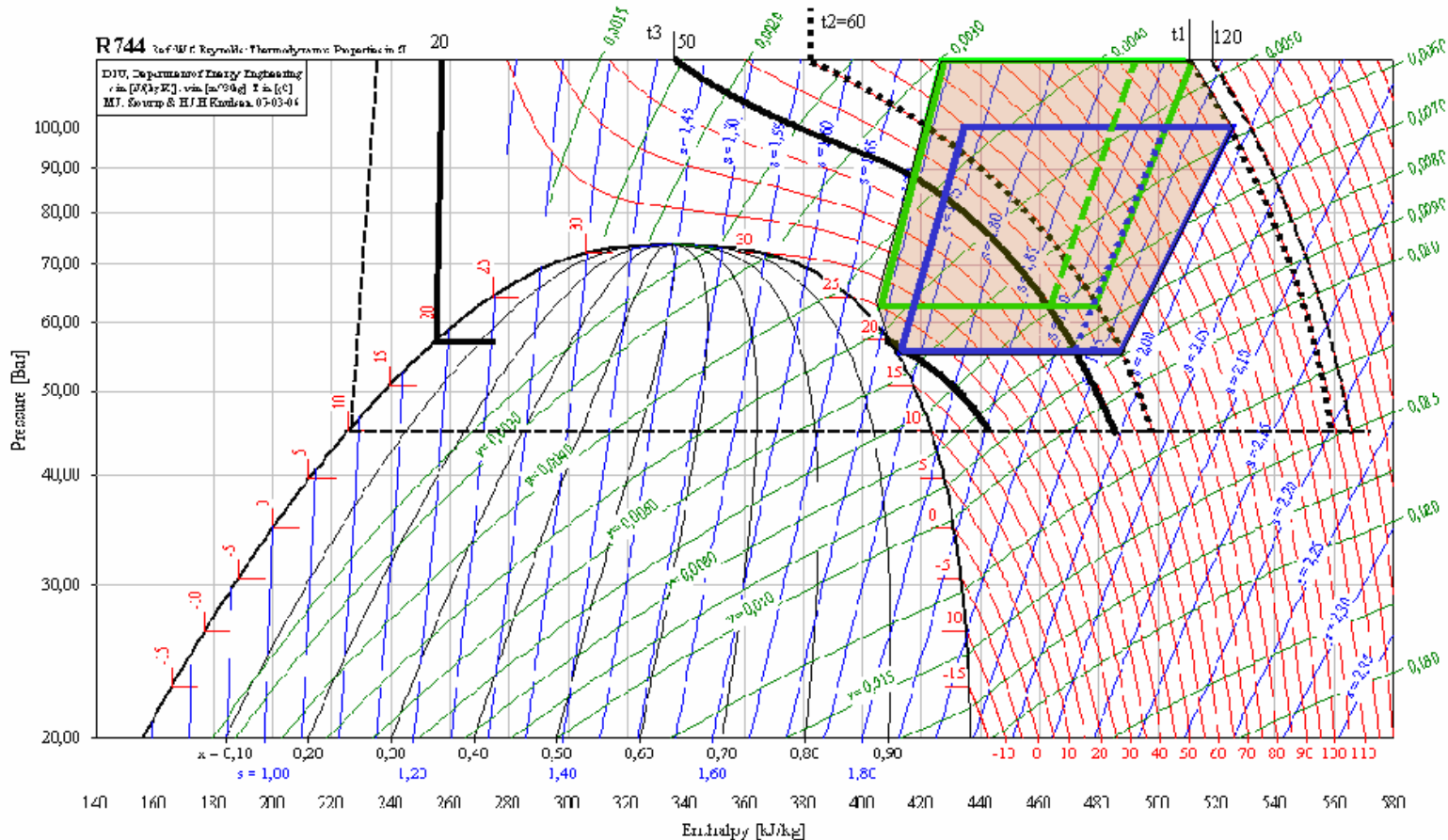


The studied heat cycles, producing simultaneously electrical power and hot tap water were limited by following curves:

isobaric curve: $p_1 = p_4 = 120$ bar;
isothermal curve: $t_1 = 115^\circ\text{C}$;

isobaric curve: $p_2 = p_3 = 45$ bar
isothermal curve: $t_2 = 60^\circ\text{C}$;

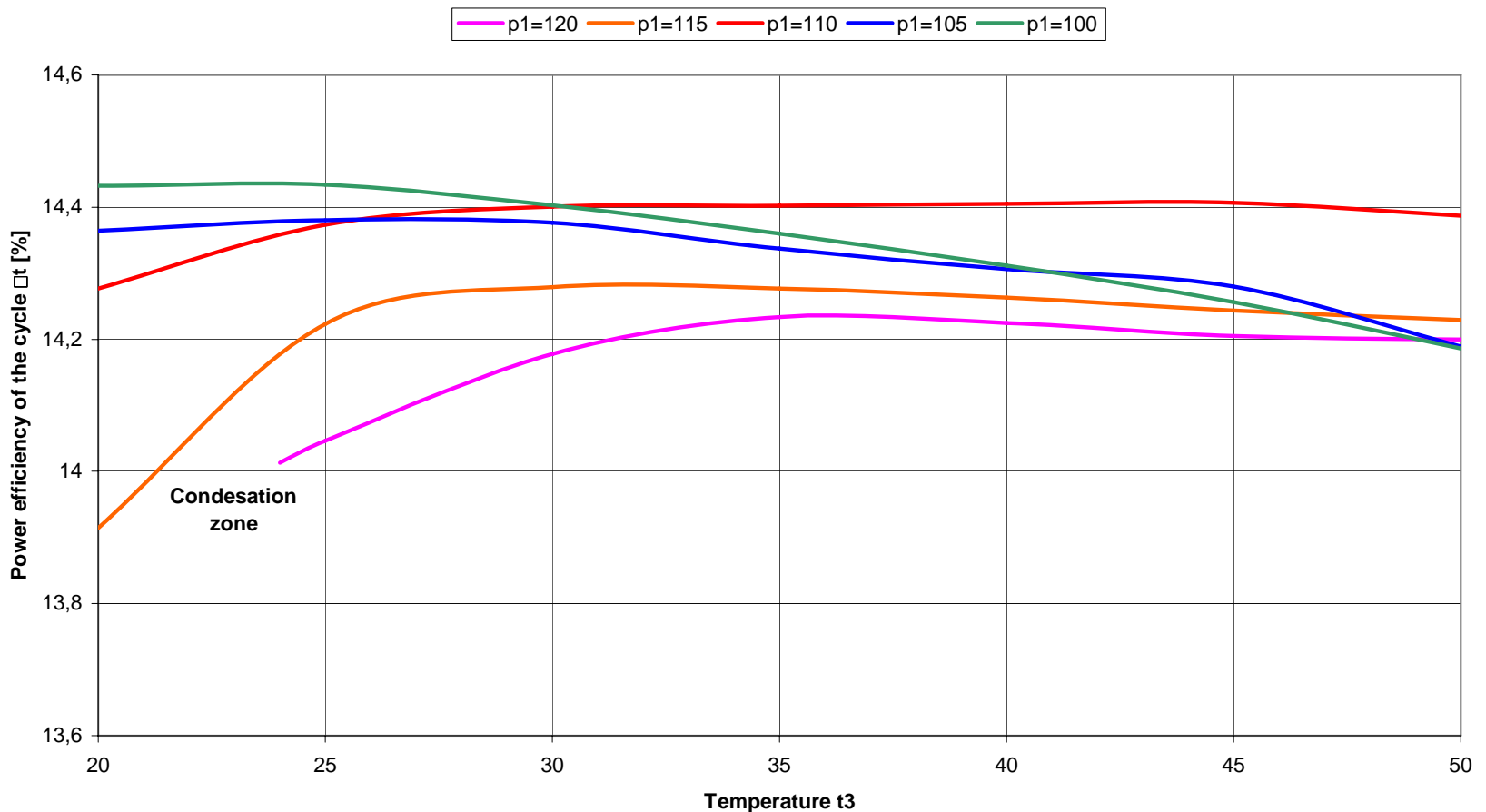
The studied parameters were the exit cooling temperature t_3 from 20 to 50 °C, and the upper pressure from 100 to 120 bar



The power efficiency is **decreasing** with the growth of upper pressure ($p_1=p_4$) presenting **no significant variation** with lowest temperature ($t_3=t_2$)

*The maximum efficiency ($\approx 14.43\%$) was provided for upper pressure **100 bar** and cooling exit temperature of **25 °C***

Power efficiency of CO₂ cycles producing electrical power and hot tap water: $t_1=115^\circ\text{C}$, $t_2=60^\circ\text{C}$



The studied heat cycles, producing simultaneously electrical power and

heating agent for district heating were limited by following curves:

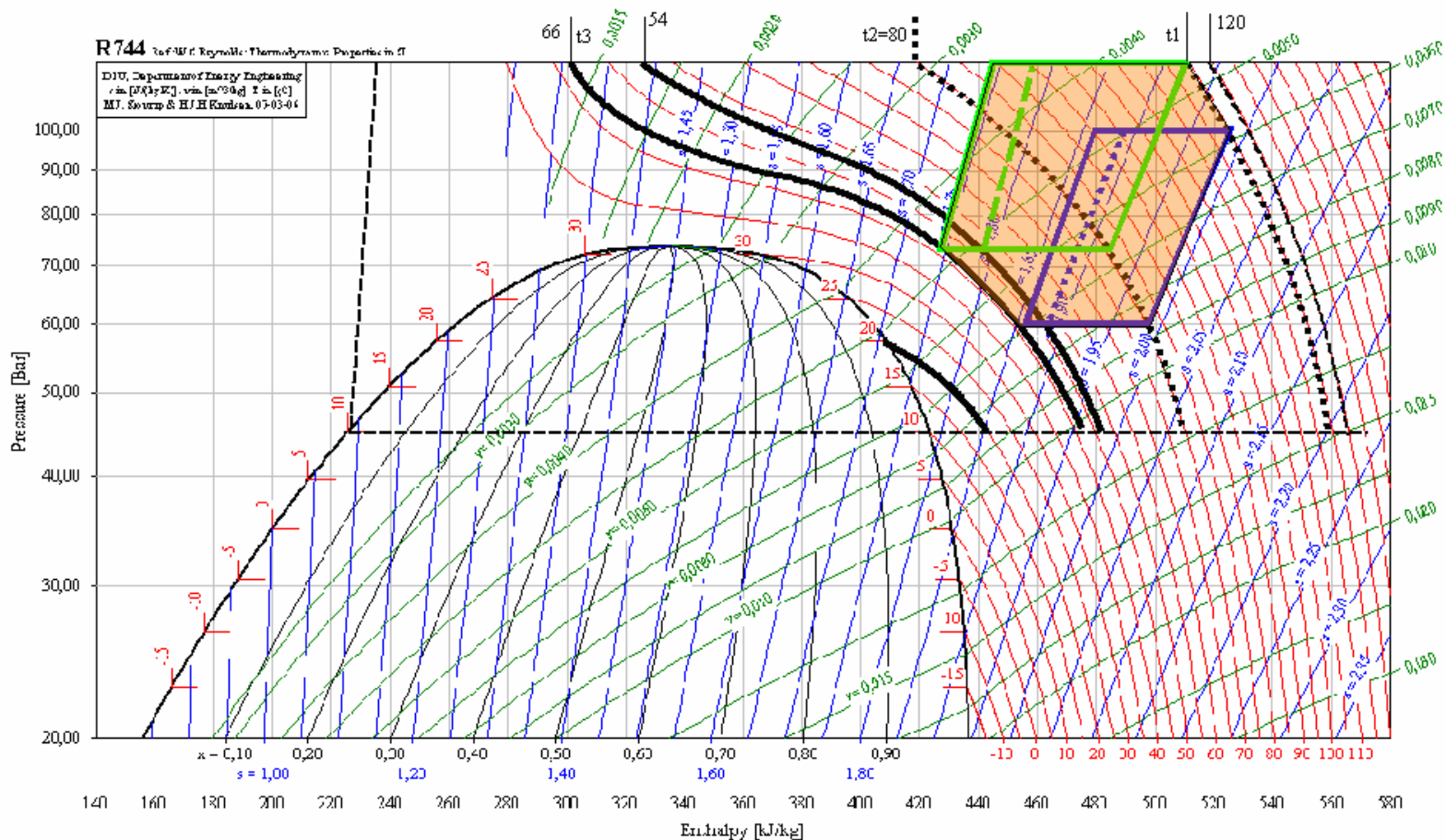
isobaric curve: $p_1 = p_4 = 120$ bar;

isothermal curve: $t_1 = 115^\circ\text{C}$;

isobaric curve: $p_2 = p_3 = 60$ bar

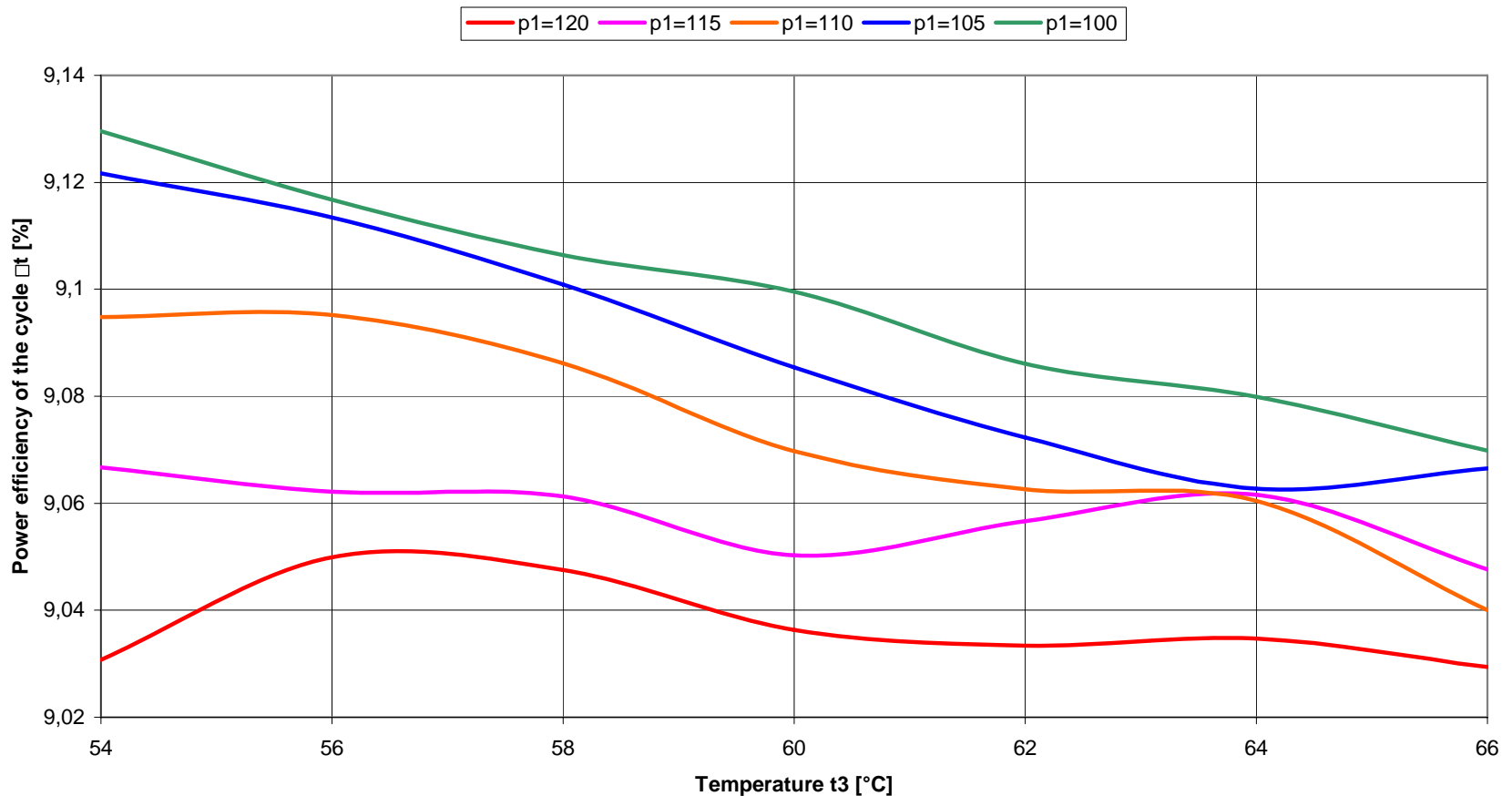
isothermal curve: $t_2 = 80^\circ\text{C}$;

The studied parameters was the exit cooling temperature t_3 from 54 to 66 °C, and the upper pressure from 100 to 120 bar



The power efficiency is decreasing with the growth of upper pressure ($p_1=p_4$) and slightly descending with growth of lowest temperature ($t_3=t_2$)
The maximum efficiency ($\approx 9.13\%$) was provided for upper pressure 100 bar and cooling lowest temperature of 54°C

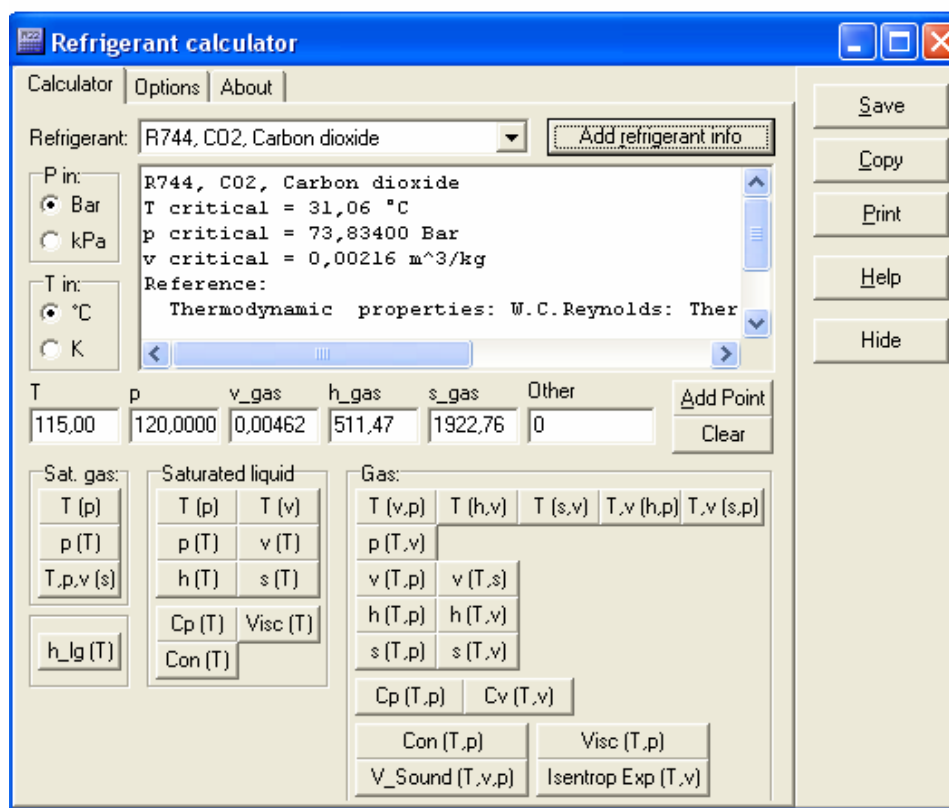
Power efficiency of CO2 cycles producing electrical power and heat agent for district heating:
 $t_1=115^\circ\text{C}$, $t_2=80^\circ\text{C}$



The study was conducted developing Excel spreadsheets using data for CO₂ properties provided by:

NATIONAL INSTITUTE OF STANDARDS AND TECHNOLOGY (NIST)

and ***COOLPACK*** software



We also developed Interpolation (User Defined) Visual Basic Function to calculate the CO₂ properties at any given state inside the limited studied field:

$$-s = s(t, p)$$

$$-h = h(p, s)$$

$$-h = h(p, t)$$

$$-t = t(p) - \text{saturation curve}$$

$$-p = p(t) - \text{saturation curve}$$

Conclusions (I)

We can use CO₂ as working fluid in power plants working on the Clausius – Rankine cycle using geothermal water as heat source, but the **thermal efficiency** is relatively low ($\approx 12,5 \%$), consisting off power efficiency only.

We can improve the power efficiency of binary cycle by :

- *Working with higher upper pressures (more than 120 bar)*
- *Lowering the temperature of condensation agent (below 10 °C)*
- *Make sure that points 2 and 3 are on the saturation curve (no cooling before condensation and no overcooling of liquid CO₂ are needed)*

Conclusions (II)

We can also use CO₂ as agent in plants working on vapour cycle using geothermal water and also producing **hot tap water** in CO₂ cooling process.

The **thermal efficiency** is theoretically high (100%), consisting off **power efficiency** (14,4%), and **heating efficiency** (85,6%).

The same sort of cycles may be used for plants producing electrical power and **heating agent for district heating** in CO₂ cooling process.

The **thermal efficiency** is theoretically the same (100%), consisting off **power efficiency** (9,14%), and **heating efficiency** (91,86%).

We can improve the power efficiency of the vapour cycle by

- *Working with higher upper temperatures, if possible (more than 115 °C)*
- *Working with moderate upper pressures (100 °bar)*